

31E

$$1) 10^4 = 10,000$$

$$2) \sqrt{25} = 5 \quad 5^3 = 125$$

$$3) 13^1 = 13$$

$$4) \sqrt{16} = 4 \quad 4^3 = 64$$

$$5) A^{3/3} = A^1 \text{ or } A$$

$$6) 3^{1/2} \cdot 3^3 = 3^{7/2}$$

$$7) X^{5/6} \cdot X^{3/6} = X^{8/6} = X^{4/3}$$

$$8) 2^{2/6} \cdot 2^{3/6} \cdot 2^{7/6} = 2^{12/6} = 2^2 = 4$$

$$9) \frac{10 \text{ m}}{1} \times \frac{1.1 \text{ yd.}}{1 \text{ m}} = 11 \text{ yd.}$$

$$10) \frac{20 \text{ kg}}{1} \times \frac{2.2 \text{ lbs}}{1 \text{ kg}} = 44 \text{ lbs.}$$

$$11) \frac{2 \text{ ft}^3}{1} \times \frac{12 \text{ in.}}{1 \text{ ft}} \times \frac{12 \text{ in.}}{1 \text{ ft}} \times \frac{12 \text{ in.}}{1 \text{ ft}} \\ = 2,456 \text{ in.}^3$$

$$12) \frac{14 \text{ yd.}^3}{1} \times \frac{3 \text{ ft.}}{1 \text{ yd.}} \times \frac{3 \text{ ft.}}{1 \text{ yd.}} \times \frac{3 \text{ ft.}}{1 \text{ yd.}} \\ = 378 \text{ ft.}^3$$

$$13) (5A + 5B)(5A + 5B) = \\ 25A^2 + 50AB + 25B^2$$

$$14) X^3 + X^2Y + XY^2 - X^2Y - XY^2 - Y^3 = \\ X^3 - Y^3$$

$$15) 4X^2 + 10X + 6$$

$$16) 6 + Y = 2X \Rightarrow Y - 2X = -6 \\ -3(Y - 2X = -6) \Rightarrow -3Y + 6X = 18$$

$$\begin{array}{rcl} 3Y - 4X = 2 & & 6 + Y = 2(10) \\ -3Y + 6X = 18 & & 2X = 20 \\ \hline 2X = 20 & & 6 + Y = 20 \\ X = 10 & & Y = 14 \\ & & (10, 14) \end{array}$$

$$17) \frac{586,400 \text{ mi.}^2}{1} \times \frac{27,878,400 \text{ ft.}^2}{1 \text{ mi.}^2} \\ = 16,347,893,760,000 \text{ ft.}^2$$

$$18) 16,347,893,760,000 \div 6,000,000,000 = \\ 2,724.6 \text{ ft.}^2$$

$$19) 100 \times 100 \times 50 = 500,000 \text{ ft.}^3 \\ 500,000 \times 62 = 31,000,000 \text{ lbs.}$$

$$20) \frac{31,000,000 \text{ lbs.}}{1} \times \frac{1 \text{ ton}}{2000 \text{ lbs.}} \\ = 15,500 \text{ tons}$$

32A

$$1) 5 \times 10^5$$

$$2) 3.56 \times 10^8$$

$$3) 5.48 \times 10^7$$

$$4) 9.6 \times 10^{-4}$$

$$5) 4.68 \times 10^{-3}$$

$$6) 9.13 \times 10^{-8}$$

$$7) \approx 1.2 \times 10^{12}$$

$$(1.9 \times 10^5)(6 \times 10^6) \\ (1.9 \times 6)(10^5 \times 10^6) = 11.4 \times 10^{11} = \\ 1 \times 10^{12} \checkmark$$

$$8) \approx 8 \times 10^{14}$$

$$(1.815 \times 10^5)(4.16 \times 10^9) \\ (1.815 \times 4.16)(10^5 \times 10^9) = 7.5504 \times 10^{14} \approx \\ 7.55 \times 10^{14} \checkmark$$

$$9) \approx 3 \times 10^{13}$$

$$(8.6 \times 10^5)(3.64 \times 10^7) \\ (8.6 \times 3.64)(10^5 \times 10^7) = 31.304 \times 10^{12} = \\ 3.1304 \times 10^{13} \approx 3.1 \times 10^{13} \checkmark$$

$$10) \approx 8 \times 10^5$$

$$(8.5 \times 10^{-5})(9 \times 10^9) \\ (8.5 \times 9)(10^{-5} \times 10^9) = 76.5 \times 10^4 = \\ 7.65 \times 10^5 = 8 \times 10^5 \checkmark$$

$$11) \approx 5 \times 10^1$$

$$(9.3 \times 10^{-4})(5 \times 10^4) \\ (9.3 \times 5)(10^{-4} \times 10^4) = 46.5 \times 10^0 = \\ 4.65 \times 10^1 = 5 \times 10^1 \checkmark$$

$$12) \approx 8 \times 10^{-7}$$

$$(2.1 \times 10^{-3})(3.50 \times 10^{-4}) \\ (2.1 \times 3.50)(10^{-3} \times 10^{-4}) = 7.35 \times 10^{-7} \approx \\ 7.4 \times 10^{-7} \checkmark$$

$$13) \approx 1 \times 10^{-4}$$

$$(5.6 \times 10^5) \div (4 \times 10^9) \\ (5.6 \div 4)(10^5 \div 10^9) = 1.4 \times 10^{-4} = \\ 1 \times 10^{-4} \checkmark$$

$$14) \approx 4$$

$$(9.8 \times 10^6) \div (2.45 \times 10^6) \\ (9.8 \div 2.45)(10^6 \div 10^6) = 4.0 \times 10^0 = \\ 4.0 \checkmark$$

$$15) \approx 3 \times 10^{-1}$$

$$(3.6 \times 10^{-3}) \div (1.2 \times 10^{-2}) \\ (3.6 \div 1.2)(10^{-3} \div 10^{-2}) = 3.0 \times 10^{-1} \checkmark$$

32B

$$1) 6 \times 10^5$$

$$2) 8.54 \times 10^8$$

$$3) 6.28 \times 10^7$$

$$4) 9.5 \times 10^{-5}$$

$$5) 5.28 \times 10^{-3}$$

$$6) 9.21 \times 10^{-7}$$

$$7) \approx 9 \times 10^{11}$$

$$(1.8 \times 10^5)(5 \times 10^6) \\ (1.8 \times 5)(10^5 \times 10^6) = 9.0 \times 10^{11} = \\ 9 \times 10^{11} \checkmark$$

$$8) \approx 3 \times 10^{12}$$

$$(9.15 \times 10^5)(3 \times 10^6) \\ (9.15 \times 3)(10^5 \times 10^6) = 27.45 \times 10^{11} = \\ 3 \times 10^{12} \checkmark$$

$$9) \approx 4 \times 10^{12}$$

$$(9.6 \times 10^4)(4.36 \times 10^7) \\ (9.6 \times 4.36)(10^4 \times 10^7) = 41.856 \times 10^{11} = \\ 4.1856 \times 10^{12} \approx 4.2 \times 10^{12} \checkmark$$

$$10) \approx 7 \times 10^5$$

$$(7.5 \times 10^{-5})(9 \times 10^9) \\ (7.5 \times 9)(10^{-5} \times 10^9) = 67.5 \times 10^4 = \\ 6.75 \times 10^5 = 7 \times 10^5 \checkmark$$

$$11) \approx 5 \times 10^0$$

$$(7.9 \times 10^{-5})(6.25 \times 10^4) \\ (7.9 \times 6.25)(10^{-5} \times 10^4) = 49.375 \times 10^{-1} = \\ 4.9375 \times 10^0 \approx 4.9 \times 10^0 \text{ or } 4.9 \checkmark$$

$$12) \approx 1 \times 10^{-10}$$

$$(3.1 \times 10^{-4})(4 \times 10^{-7}) \\ (3.1 \times 4)(10^{-4} \times 10^{-7}) = 12.4 \times 10^{-11} = \\ 1.24 \times 10^{-10} = 1 \times 10^{-10} \checkmark$$

$$13) \approx 1 \times 10^{-3}$$

$$(5.2 \times 10^4) \div (4 \times 10^7) \\ (5.2 \div 4)(10^4 \div 10^7) = 1.3 \times 10^{-3} = \\ 1 \times 10^{-3} \checkmark$$

$$14) \approx 4 \times 10^{-4}$$

$$(2.4 \times 10^7) \div (6 \times 10^{10}) \\ (2.4 \div 6)(10^7 \div 10^{10}) = .4 \times 10^{-3} = \\ 4 \times 10^{-4} \checkmark$$

$$15) \approx 5 \times 10^{-2}$$

$$(3.5 \times 10^{-4}) \div (7 \times 10^{-3}) \\ (3.5 \div 7)(10^{-4} \div 10^{-3}) = .5 \times 10^{-1} = \\ 5 \times 10^{-2} \checkmark$$

32C

1) 7×10^5

15) $\frac{10 \text{ km}}{1} \times \frac{1 \text{ mi.}}{1.61 \text{ km}} = 6.21 \text{ miles}$

2) 7.6×10^{-3}

16) $\frac{75 \text{ g}}{1} \times \frac{.035 \text{ oz.}}{1 \text{ g}} = 2.625 \text{ oz.}$

3) $\approx 40,000,000,000 \text{ or } 4 \times 10^{10}$
 $(5 \times 10^3)(8 \times 10^6)$

4) $(5 \times 8)(10^3 \times 10^6) = 40 \times 10^9$

17) $(3X - 3Y)(3X - 3Y)$
 $9X^2 - 18XY + 9Y^2$

5) 4×10^{10} (significant digits correct)

6) check with calculator

7) $\approx 500 \text{ or } 5 \times 10^2$
 $(6.13 \times 10^4) \div (1.2 \times 10^2)$

8) $(6.13 \div 1.2)(10^4 \div 10^2) = 5.108 \times 10^2$

9) 5.1×10^2 (significant digits correct)

10) check with calculator

11) $(10^3)^{2/3} = 10^2$
 $10^2 \cdot 10^2 \cdot 10^{-3} = 10^1 \text{ or } 10$

12) $(2^3)^{2/3} = 2^2$
 $2^2 \cdot 2^2 = 2^4 = 16$

13) $10^{1/3} \cdot 10^3 \cdot 10^{-1} = 10^{7/3}$

14) $A^{10/2} \cdot A^{-1/2} \cdot A^{-3/2} = A^3$

32D

1) 5.86×10^8

14) $\frac{500 \text{ g}}{1} \times \frac{.035 \text{ oz.}}{1 \text{ g}} = 17.5 \text{ oz.}$

2) 5.95×10^{-4}

15) $D^3 + 5D^2 + 25D - 5D^2 - 25D - 125 =$
 $D^3 - 125$

3) $\approx 126 \text{ or } 1.26 \times 10^2$
 $(1.8 \times 10^4)(7.2 \times 10^{-3})$

16) $A^2 - AT + T^2$

4) $(1.8 \times 7.2)(10^4 \times 10^{-3}) = 12.96 \times 10^1$

17) $X(5X - 10) = 0$
 $X = 0, X = 2$

$(0)[5(0) - 10] = 0$
 $0 = 0$

$(2)[5(2) - 10] = 0$
 $2(10 - 10) = 0$
 $2(0) = 0$
 $0 = 0$

5) 1.296×10^2 with significant digits 1.3×10^2

6) check with calculator

18) $X^2 + 7X - 60 = 0$
 $(X + 12)(X - 5) = 0$
 $X = -12, X = 5$

$(-12)^2 + 7(-12) - 18 = 42$
 $144 - 84 - 18 = 42$
 $42 = 42$

$(5)^2 + 7(5) - 18 = 42$
 $25 + 35 - 18 = 42$
 $42 = 42$

7) $\approx 4800 \text{ or } 4.8 \times 10^3$
 $(1.45 \times 10^6) \div (2.9 \times 10^2)$

8) $(1.45 \div 2.9)(10^6 \div 10^2) = .5 \times 10^4$

9) 5.0×10^3 (significant digits correct)

10) check with calculator

19) $10N + 2(N + 2) - 4(N + 4) + 8 = 3(N + 4) - 11$
 $10N + 2N + 4 - 4N - 16 + 8 = 3N + 12 - 11$
 $8N - 4 = 3N + 1$

$N = 5$
 $N = 1, 3, 5$

11) $5^{-2} \cdot 5^0 \cdot 5^2 = 5^0 = 1$

20) $.10D + .05N = 1.35$
 $D + N = 16$

$10D + 5N = 135$
 $-5D - 5N = -80$

 $5D = 55$
 $D = 11$
 $(11) + N = 16$
 $N = 5$

12) $3^3 \cdot 3^3 \cdot 3^1 = 3^7$

13) $\frac{26 \text{ mi.}}{1} \times \frac{1.6 \text{ km}}{1 \text{ mi.}} = 41.6 \text{ km}$

1) 2.38×10^7

14) $\frac{2.1}{1} \times \frac{1.06 \text{ qts.}}{1} = 2.12 \text{ qts.}$

2) 1.12×10^{-7}

15) $(X - B)(X + B)$

3) $\approx 600,000 \text{ or } 6 \times 10^5$
 $(9.2 \times 10^{-1})(6.4 \times 10^5)$

4) $(9.2 \times 6.4)(10^{-1} \times 10^5) = 58.88 \times 10^4$

5) 5.888×10^5 with significant digits 5.9×10^5

6) check with calculator

7) $\approx 100 \text{ or } 1 \times 10^2$
 $(4 \times 10^{-1})(2.5 \times 10^{-1}) \div (1 \times 10^{-3})$

8) $(4 \times 2.5 \div 1)(10^{-1} \times 10^{-1} \div 10^{-3}) = 10 \times 10^1$

9) 1×10^2 (significant digits correct)

10) check with calculator

11) $A^{9/12} \cdot A^{16/12} = A^{25/12}$

12) $3^1 \cdot 3^2 \cdot 3^4 = 3^7$

13) $\frac{100 \text{ m}}{1} \times \frac{1.1 \text{ yds.}}{1 \text{ m}} = 110 \text{ yds.}$

16) $4X(X^4 - 81)$

$4X(X^2 - 9)(X^2 + 9)$
 $4X(X - 3)(X + 3)(X^2 + 9)$

17) $X^2 + X - 72 = 0$

$(X + 9)(X - 8) = 0$
 $X = -9, X = 8$

$(-9)^2 + (-9) - 12 = 60$
 $81 - 9 - 12 = 60$
 $60 = 60$
 $(8)^2 + (8) - 12 = 60$
 $64 + 8 - 12 = 60$
 $60 = 60$

18) $(2 - A)(2 + A) = 0$
 $A = 2, A = -2$

$4 - (-2)^2 = 0$
 $4 - 4 = 0$
 $4 - (2)^2 = 0$
 $4 - 4 = 0$

19) $\frac{9.5 \times 10^6 \text{ mi}^2}{1} \times \frac{5.28 \times 10^3 \text{ ft.}}{1 \text{ mi.}} \times \frac{5.28 \times 10^3 \text{ ft.}}{1 \text{ mi.}}$

$= 265 \times 10^{12} = 2.65 \times 10^{14} \text{ sq. ft.}$

with significant digits 2.6×10^{14} sq. ft. or
 2.7×10^{14} sq. ft. depending on when
rounding was done.

20) $(2.65 \times 10^{14} \text{ sq. ft.}) \div (6 \times 10^9 \text{ people}) =$
 $(2.65 \div 6)(10^{14} \div 10^9) = .44 \times 10^5 =$
 $4.4 \times 10^4 \text{ sq. ft. per person}$

1 acre $\approx 4.4 \times 10^4$ sq. ft. so 1 acre per person

1) $3^3 = 27$
 $27 \overline{)80} \quad 9 \overline{)26} \quad 3 \overline{)8} \quad 1 \overline{)2}$
 $\underline{27} \quad \underline{18} \quad \underline{6} \quad \underline{2}$
 $26 \quad 8 \quad 2 \quad 0$

22223

2) $5^2 = 25$
 $25 \overline{)80} \quad 5 \overline{)5} \quad 1 \overline{)0}$
 $\underline{25} \quad \underline{5} \quad \underline{0}$
 $5 \quad 0 \quad 0$

3105

3) $4^3 = 64$
 $64 \overline{)80} \quad 16 \overline{)16} \quad 4 \overline{)0} \quad 1 \overline{)0}$
 $\underline{64} \quad \underline{16} \quad \underline{0} \quad \underline{0}$
 $16 \quad 0 \quad 0 \quad 0$

11004

4) $6^2 = 36$
 $36 \overline{)100} \quad 6 \overline{)28} \quad 1 \overline{)4}$
 $\underline{36} \quad \underline{24} \quad \underline{4}$
 $28 \quad 4 \quad 0$

2446

5) $8^3 = 512$
 $512 \overline{)1352} \quad 64 \overline{)328} \quad 8 \overline{)3} \quad 1 \overline{)0}$
 $\underline{512} \quad \underline{320} \quad \underline{8} \quad \underline{0}$
 $328 \quad 8 \quad 0 \quad 0$

25108

6) $6^4 = 1296$
 $1296 \overline{)1352} \quad 216 \overline{)56} \quad 36 \overline{)56} \quad 6 \overline{)18}$
 $\underline{1296} \quad \underline{56} \quad \underline{36} \quad \underline{18}$
 $56 \quad 0 \quad 20 \quad 2$

101326

7) $5 \times 7^2 + 6 \times 7^1 + 3 \times 7^0$
 $5(49) + 6(7) + 3(1) =$
 $245 + 42 + 3 = 290$

8) $4 \times 5^2 + 4 \times 5^1 + 1 \times 5^0$
 $4(25) + 4(5) + 1(1) =$
 $100 + 20 + 1 = 121$

9) $2 \times 3^3 + 1 \times 3^2 + 2 \times 3^1 + 1 \times 3^0$
 $2(27) + 1(9) + 2(3) + 1(1) =$
 $54 + 9 + 6 + 1 = 70$

10) $3 \times 5^3 + 4 \times 5^2 + 2 \times 5^1 + 1 \times 5^0$
 $3(125) + 4(25) + 2(5) + 1(1) =$
 $375 + 100 + 10 + 1 = 486$

11) $6 \times (12^2 + 10 \times (12)^1 + 8 \times (12)^0)$
 $6(144) + 10(12) + 8(1) =$
 $864 + 120 + 8 = 992$

12) $11 \times (13)^2 + 8 \times (13)^1 + 1 \times (13)^0$
 $11(169) + 8(13) + 1(1) =$
 $1859 + 104 + 1 = 1964$

Problem in Student Text was rewritten after first printing.
This is a solution for E8113 = 0

$$1) \begin{aligned} -5A + 3 + 8A - 4 &= 9 + 3 - 1 \\ (-5A + 8A) + (3 - 4) &= 11 \\ 3A + (-1) &= 11 \\ +1 &+1 \\ \hline A &= 4 \end{aligned}$$

Check: $-5(4) + 3 + 8(4) - 4 = 9 + 3 - 1$
 $-20 + 3 + 32 - 4 = 9 + 3 - 1$
 $11 = 11$

Checks for #2 - #14 will not be shown.

$$2) \begin{aligned} 3B - B + 7 + 4B &= 43 \\ 6B + 7 &= 43 \\ -7 &-7 \\ \hline 6B &= 36 \\ \frac{6B}{6} &= \frac{36}{6} \\ B &= 6 \end{aligned}$$

$$3) \begin{aligned} -4Y - 6 + 7Y + 3 + Y &= 17 \\ 4Y - 3 &= 17 \\ +3 &+3 \\ \hline 4Y &= 20 \\ \frac{4Y}{4} &= \frac{20}{4} \\ Y &= 5 \end{aligned}$$

$$4) \begin{aligned} 5Q + 3Q - 6 + 2Q &= (2 + 3) + 9 \\ 10Q - 6 &= 14 \\ +6 &+6 \\ \hline 10Q &= 20 \\ \frac{10Q}{10} &= \frac{20}{10} \\ Q &= 2 \end{aligned}$$

$$5) \begin{aligned} 6K - 5 + 4K - K + 2 &= 12 \cdot 2 \\ 9K - 3 &= 24 \\ +3 &+3 \\ \hline 9K &= 27 \\ \frac{9K}{9} &= \frac{27}{9} \\ K &= 3 \end{aligned}$$

$$6) \begin{aligned} 5C - 2C - 8 + 7 - C &= 4 + 1 \\ 2C - 1 &= 13 \\ +1 &+1 \\ \hline 2C &= 14 \\ \frac{2C}{2} &= \frac{14}{2} \\ C &= 7 \end{aligned}$$

$$7) \begin{aligned} 4A + 6 - 2A + 12 &\\ 4A - 2A &= 12 - 6 \\ \frac{2A}{2} &= \frac{6}{2} \\ A &= 3 \end{aligned}$$

$$8) \begin{aligned} 10B - 2B + 3 &= 5B + 21 \\ 8B - 5B &= 21 - 3 \\ \frac{3B}{3} &= \frac{18}{3} \\ B &= 6 \end{aligned}$$

$$9) \begin{aligned} 6C - 8 + 3C &= 70 - 2C + 12 \\ 9C - 5C &= 72 + 8 \\ \frac{4C}{4} &= \frac{20}{4} \\ C &= 5 \end{aligned}$$

$$10) \begin{aligned} 5D - 10 &= -2D - 34 \\ 6D + 2D &= -34 + 10 \\ \frac{8D}{8} &= \frac{-24}{8} \\ D &= -3 \end{aligned}$$

$$11) \begin{aligned} -3A - 3 - 6A + 10A + 5 &= 10 \\ A + 2 &= 10 \\ -2 &-2 \\ \hline A &= 8 \\ A &= 8 \end{aligned}$$

$$12) \begin{aligned} -5B - B + 4 + 10B - 7 &= 7 \cdot 11 \\ 4B - 3 &= 77 \\ +3 &+3 \\ \hline 4B &= 80 \\ \frac{4B}{4} &= \frac{80}{4} \\ B &= 20 \end{aligned}$$

$$13) \begin{aligned} -4R + 7R - 3 + 5R &= 10^2 - 7 \\ 8R &= 100 - 7 + 3 \\ 8R &= 96 \\ \frac{8R}{8} &= \frac{96}{8} \\ R &= 12 \end{aligned}$$

$$14) \begin{aligned} -7Q + 8 - 6 + 5Q &= 3 \cdot 5 - 7 \\ -2Q + 2 &= 8 \\ -2 &-2 \\ \hline -2Q &= 6 \\ \frac{-2Q}{-2} &= \frac{6}{-2} \\ Q &= -3 \end{aligned}$$