

20E

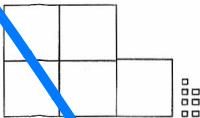
1) $\frac{x^2 + 3x - 2}{x^2 + x + 3}$

$$\frac{2x^2 + 7x + 1}{2x^2 + 7x + 1}$$



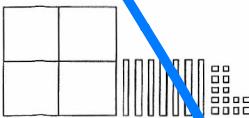
2) $\frac{3x^2 + 2x - 1}{5x^2 - 2x + 8}$

$$\frac{2x^2 - 2x + 7}{5x^2 + 7}$$

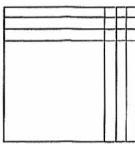


3) $\frac{5x^2 + 4x + 7}{-x^2 + 3x + 7}$

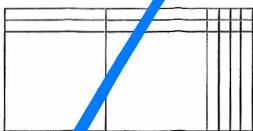
$$\frac{-4x^2 + 7x + 14}{4x^2 + 7x + 14}$$



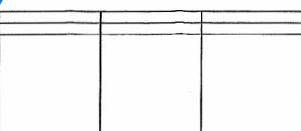
4) $(x+3)(x+3) = x^2 + 6x + 9$



5) $(2x+4)(x+2) = 2x^2 + 8x + 8$



6) $(3x)(x+2) = 3x^2 + 6x$



7) $\frac{2x - 3}{2x^2 - 3x}$

$$\frac{x}{2x^2 - 7x + 6}$$

8) $\frac{x - 1}{x^2 - x}$

$$\frac{-6x + 6}{x^2 - 7x + 6}$$

9) $\frac{2x + 2}{-6x - 6}$

$$\frac{x}{2x^2 + 2x}$$

10) x^{-5}

11) $\frac{1}{y^2}$

12) $7 \cdot 2 + 5 \cdot (-2) = 75$

13) $A^7 B^{-3}$

14) $5^2 \cdot 5 = 5^{10}$

15) $(5^3)^4$

16) $+3, -13$

17) $C^{-4} \cdot B^3 D^{-3+8-7} = C^{-1} D^{-2}$

18) $\frac{3n+4}{5n+9}$

19) $5(10) + 9 = 559$

20) $\frac{2y+7}{10y+35}$

$$\frac{7y+5}{14y^2 + 49y}$$

$$\frac{14y^2 + 59y + 35}{14y^2 + 59y + 35}$$

21A

1) $\frac{x+2}{x+2}$

$$\frac{x}{2x+4}$$

$$\frac{x^2+2x}{x^2+4x+4}$$

2) $\frac{x+3}{x+2}$

$$\frac{x}{2x+6}$$

$$\frac{x^2+3x}{x^2+5x+6}$$

3) $\frac{x+10}{x+1}$

$$\frac{x}{x+10}$$

$$\frac{x^2+10x}{x^2+11x+10}$$

4) $\frac{x+4}{x+2}$

$$\frac{x}{2x+8}$$

$$\frac{x^2+4x}{x^2+6x+8}$$

5) $\frac{x+7}{x+1}$

$$\frac{x}{x+7}$$

$$\frac{x^2+7x}{x^2+8x+7}$$

6) $\frac{x+6}{x+2}$

$$\frac{x}{2x+12}$$

$$\frac{x^2+6x}{x^2+8x+12}$$

7) $\frac{x+11}{x+1}$

$$\frac{x}{x+11}$$

$$\frac{x^2+11x}{x^2+12x+11}$$

8) $\frac{x+6}{x+1}$

$$\frac{x}{x+6}$$

$$\frac{x^2+2x}{x^2+7x+6}$$

9) $\frac{x+7}{x+2}$

$$\frac{x}{2x+14}$$

$$\frac{x^2+7x}{x^2+9x+14}$$

10) $\frac{x+15}{x+1}$

$$\frac{x}{x+15}$$

$$\frac{x^2+15x}{x^2+16x+15}$$

11) $\frac{x+2}{x+1}$

$$\frac{x}{x+2}$$

$$\frac{x^2+2x}{x^2+3x+2}$$

12) $\frac{x+3}{x+1}$

$$\frac{x}{x+3}$$

$$\frac{x^2+3x}{x^2+4x+3}$$

13) $\frac{x+8}{x+1}$

$$\frac{x}{x+8}$$

$$\frac{x^2+8x}{x^2+9x+8}$$

14) $\frac{x+18}{x+1}$

$$\frac{x}{x+18}$$

$$\frac{x^2+18x}{x^2+19x+18}$$

15) $\frac{x+5}{x+4}$

$$\frac{x}{4x+20}$$

$$\frac{x^2+5x}{x^2+9x+20}$$

16) $\frac{x+7}{x+3}$

$$\frac{x}{3x+21}$$

$$\frac{x^2+7x}{x^2+10x+21}$$

21B

1)
$$\begin{array}{r} X+8 \\ \times X+2 \\ \hline 2X+16 \\ X^2+8X \\ \hline X^2+10X+16 \end{array}$$

2)
$$\begin{array}{r} X+7 \\ \times X+4 \\ \hline 4X+28 \\ X^2+7X \\ \hline X^2+11X+28 \end{array}$$

3)
$$\begin{array}{r} X+11 \\ \times X+2 \\ \hline 2X+22 \\ X^2+11X \\ \hline X^2+13X+22 \end{array}$$

4)
$$\begin{array}{r} X+4 \\ \times X+3 \\ \hline 3X+12 \\ X^2+4X \\ \hline X^2+7X+12 \end{array}$$

5)
$$\begin{array}{r} X+5 \\ \times X+3 \\ \hline 3X+15 \\ X^2+5X \\ \hline X^2+8X+15 \end{array}$$

6)
$$\begin{array}{r} X+6 \\ \times X+5 \\ \hline 5X+30 \\ X^2+6X \\ \hline X^2+11X+30 \end{array}$$

7)
$$\begin{array}{r} X+4 \\ \times X+1 \\ \hline X+4 \\ X^2+4X \\ \hline X^2+5X+4 \end{array}$$

8)
$$\begin{array}{r} X+5 \\ \times X+1 \\ \hline X+5 \\ X^2+5X \\ \hline X^2+6X+5 \end{array}$$

9)
$$\begin{array}{r} X+4 \\ \times X+4 \\ \hline 4X+16 \\ X^2+4X \\ \hline X^2+8X+16 \end{array}$$

10)
$$\begin{array}{r} X+10 \\ \times X+2 \\ \hline 2X+20 \\ X^2+10X \\ \hline X^2+12X+20 \end{array}$$

11)
$$\begin{array}{r} X+9 \\ \times X+2 \\ \hline 2X+18 \\ X^2+9X \\ \hline X^2+11X+18 \end{array}$$

12)
$$\begin{array}{r} X+15 \\ \times X+2 \\ \hline 2X+30 \\ X^2+15X \\ \hline X^2+17X+30 \end{array}$$

13)
$$\begin{array}{r} X+5 \\ \times X+2 \\ \hline 2X+10 \\ X^2+5X \\ \hline X^2+7X+10 \end{array}$$

14)
$$\begin{array}{r} X+1 \\ \times X+1 \\ \hline X+1 \\ X^2+X \\ \hline X^2+2X+1 \end{array}$$

15)
$$\begin{array}{r} X+5 \\ \times X+5 \\ \hline 5X+25 \\ X^2+5X \\ \hline X^2+10X+25 \end{array}$$

16)
$$\begin{array}{r} X+25 \\ \times X+1 \\ \hline X+25 \\ X^2+5X \\ \hline X^2+6X+5 \end{array}$$

Check using same method as other examples.

21C

1)
$$X^2 + 7X + 12 = (X + 4)(X + 3)$$

$$\begin{array}{r} X+4 \\ \times X+3 \\ \hline 3X+12 \\ X^2+4X \\ \hline X^2+7X+12 \end{array}$$

2)
$$X^2 + 10X + 16 = (X + 8)(X + 2)$$

$$\begin{array}{r} X+8 \\ \times X+2 \\ \hline 2X+20 \\ X^2+10X \\ \hline X^2+12X+20 \end{array}$$

3)
$$X^2 + 11X + 24 = (X + 8)(X + 3)$$

$$\begin{array}{r} X+8 \\ \times X+3 \\ \hline 3X+24 \\ X^2+9X \\ \hline X^2+11X+24 \end{array}$$

4)
$$X^2 + 8X + 12 = (X + 6)(X + 2)$$

$$\begin{array}{r} X+6 \\ \times X+2 \\ \hline 2X+12 \\ X^2+4X \\ \hline X^2+8X+12 \end{array}$$

5)
$$(X + 4)(X + 2) = X^2 + 6X + 8$$

$$\begin{array}{r} X+4 \\ \times X+2 \\ \hline 2X+8 \\ X^2+4X \\ \hline X^2+6X+8 \end{array}$$

6)
$$(X + 5)(X + 3) = X^2 + 8X + 15$$

$$\begin{array}{r} X+5 \\ \times X+3 \\ \hline 3X+15 \\ X^2+5X \\ \hline X^2+8X+15 \end{array}$$

7)
$$X^2 + 7X + 6 = (X + 6)(X + 1)$$

$$\begin{array}{r} X+6 \\ \times X+1 \\ \hline X+6 \\ X^2+6X \\ \hline X^2+7X+6 \end{array}$$

9)
$$X^2 + 2X + 1 = (X + 1)(X + 1)$$

$$\begin{array}{r} X+1 \\ \times X+1 \\ \hline X+1 \\ X^2+X \\ \hline X^2+2X+1 \end{array}$$

11)
$$2X^2 - 7X - 3 = \frac{X^2 + 5X + 9}{3X^2 - 2X + 6}$$

$$\begin{array}{r} X+3 \\ \times X+2 \\ \hline 2X+6 \\ X^2+5X \\ \hline X^2+7X+3 \end{array}$$

13)
$$P-8P^4 = P-4$$

14)
$$R(-2)(-3)S(3)(-3) = R6S-9$$

15) 225

16) ±4

17)
$$11N + 2(N + 2) = 6(N + 4) + 1$$

$$11N + 2N + 4 = 6N + 25$$

$$7N = 25 - 4$$

$$N = 3 \quad 3, 5, 7$$

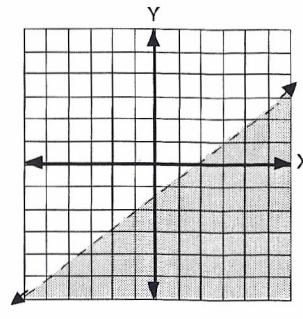
18) .10D + .05N = .60, D + N = 9

10D + 5N = 60

-5D - 5N = -45

$$\begin{array}{r} 5D = 15 \\ D = 3 \end{array} \quad (3) + N = 9 \quad N = 6$$

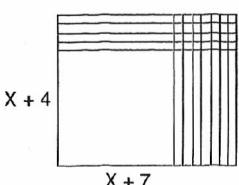
19)
$$7X - Y = -3$$



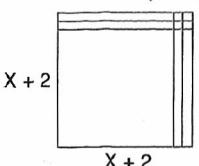
20)
$$Y < \frac{3}{4}X - \frac{5}{4}$$

21D

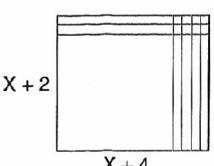
1) $X^2 + 11X + 28 = (X + 7)(X + 4)$



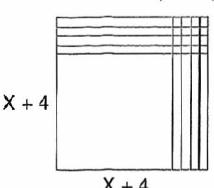
2) $X^2 + 4X + 4 = (X + 2)(X + 2)$



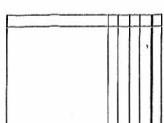
3) $X^2 + 6X + 8 = (X + 4)(X + 2)$



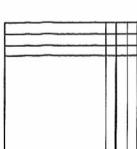
4) $X^2 + 8X + 16 = (X + 4)(X + 4)$



5) $(X + 5)(X + 1) = X^2 + 6X + 5$



6) $(X + 3)(X + 3) = X^2 + 6X + 9$



7) $X^2 + 12X + 32 = (X + 8)(X + 4)$

$$\begin{array}{r} X+8 \\ \times X+4 \\ \hline 4X+32 \\ X^2+8X \\ \hline X^2+12X+32 \end{array}$$

9) $X^2 + 20X + 100 = (X + 10)(X + 10)$

$$\begin{array}{r} X+10 \\ \times X+10 \\ \hline 10X+100 \\ X^2+10X \\ \hline X^2+20X+100 \end{array}$$

$$\begin{array}{r} X^2+X-4 \\ X^2+3X+3 \\ \hline 2X^2+4X-1 \end{array}$$

$$\begin{array}{r} 2X^2+7X+6 \\ 5X^2-4X+10 \\ \hline 7X^2+3X+16 \end{array}$$

13) $P(5)(3)(-2) = P^{-30}$

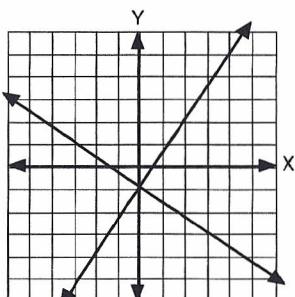
14) anything to the "0" power equals 1

15) 121

16) ± 12

17) $14(N + 2) + 4N = 12(N + 4) - 2$
 $18N + 28 = 12N + 46$
 $6N = 18$
 $N = 3 \quad 3, 5, 7$

18) $.10D + .05N = 1.80, \quad D + N = 27$
 $10D + 5N = 180$
 $-5D - 5N = -135$
 $5D = 45 \quad (9) + N = 27$
 $D = 9 \quad N = 18$

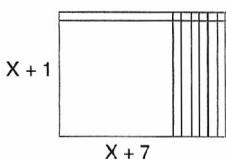


19) on the graph

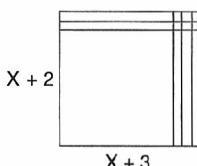
20) $m = -2/3$
 $(-3) = -2/3(3) + b$
 $b = -1$

21E

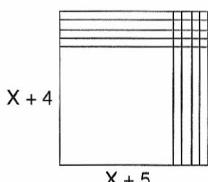
1) $X^2 + 8X + 7 = (X + 7)(X + 1)$



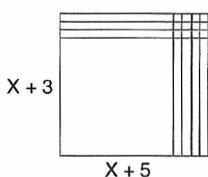
2) $X^2 + 5X + 6 = (X + 3)(X + 2)$



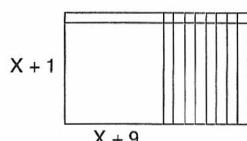
3) $X^2 + 9X + 20 = (X + 5)(X + 4)$



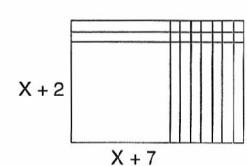
4) $X^2 + 8X + 15 = (X + 5)(X + 3)$



5) $(X + 1)(X + 9) = X^2 + 10X + 9$



6) $(X + 7)(X + 2) = X^2 + 9X + 14$



7) $X^2 + 7X + 12 = (X + 3)(X + 4)$

$$\begin{array}{r} X+3 \\ \times X+4 \\ \hline 4X+12 \\ X^2+3X \\ \hline X^2+7X+12 \end{array}$$

9) $X^2 + 10X + 21 = (X + 3)(X + 7)$

$$\begin{array}{r} X+3 \\ \times X+7 \\ \hline 7X+21 \\ X^2+3X \\ \hline X^2+10X+21 \end{array}$$

$$\begin{array}{r} 4X^2-4X+1 \\ X^2+2X-1 \\ \hline 5X^2-2X+0 \end{array}$$

$$\begin{array}{r} 2X^2+3X+3 \\ X^2+7X-2 \\ \hline 3X^2+10X+1 \end{array}$$

13) $P^{0+4-1} = P^3$

14) $S(2)(-2)R^5 = S^{-4}R^5 \quad (R^0 \text{ and } S^0 = 1)$

15) 169

16) ± 5

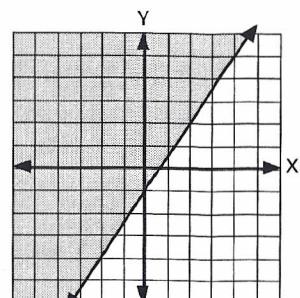
17) $(N + 1) + 7(N + 2) = 5N$
 $N + 1 + 7N + 14 = 5N$
 $8N + 15 = 5N$
 $N = -5 \quad -5, -4, -3$

18) $.01P + .05N = .76, \quad P + N = 20$

$$\begin{array}{r} P+5N=76 \\ -P-N=-20 \\ \hline 4N=56 \\ N=14 \end{array}$$

$$P + (14) = 20 \\ P = 6$$

19) $Y = -3/4 X + 4$



20) $Y \geq 3/2 X - 1$

3C

1)
$$\begin{aligned} X + 3 &= 9 \\ X + 3 - 3 &= 9 - 3 \\ X &= 6 \end{aligned}$$

2)
$$\begin{aligned} X + 6 &= 10 \\ X + 6 - 6 &= 10 - 6 \\ X &= 4 \end{aligned}$$

3)
$$\begin{aligned} 2X + 5 &= 11 \\ 2X + 5 - 5 &= 11 - 5 \\ 2X &= 6 \\ 2X \div 2 &= 6 \div 2 \\ X &= 3 \end{aligned}$$

4)
$$\begin{aligned} 4Q - 2 &= 10 \\ 4Q - 2 + 2 &= 10 + 2 \\ 4Q &= 12 \\ 4Q \div 4 &= 12 \div 4 \\ Q &= 3 \end{aligned}$$

5)
$$\begin{aligned} 4X + 2 &= 2X + 8 \\ 4X + 2 - 2 &= 2X + 8 - 2 \\ 4X &= 2X + 6 \\ 4X - 2X &= 2X - 2X + 6 \\ 2X &= 6 \\ 2X \div 2 &= 6 \div 2 \\ X &= 3 \end{aligned}$$

6)
$$\begin{aligned} 3Y + 5 &= 2Y + 7 \\ 3Y + 5 - 5 &= 2Y + 7 - 5 \\ 3Y &= 2Y + 2 \\ 3Y - 2Y &= 2Y - 2Y + 2 \\ Y &= 2 \end{aligned}$$

7)
$$\begin{aligned} Q + 4 &= 3Q - 6 \\ Q + 4 - Q &= 3Q - Q - 6 \\ 4 &= 2Q - 6 \\ 4 + 6 &= 2Q - 6 + 6 \\ 10 &= 2Q \\ 10 \div 2 &= 2Q \div 2 \\ 5 &= Q \end{aligned}$$

8)
$$\begin{aligned} 2R + 8 &= 3R - 2 \\ 2R - 2R + 8 &= 3R - 2R - 2 \\ 8 &= R - 2 \\ 8 + 2 &= R - 2 + 2 \\ 10 &= R \end{aligned}$$

9)
$$\begin{array}{rcl} 9 - 3 & \textcircled{<} & |4 - 11| \\ 6 & & |7| \\ 6 & < & 7 \end{array}$$

10)
$$\begin{array}{rcl} |1 - 2 - 3| & \textcircled{<} & |2 \times 3| \\ |-4| & & |6| \\ 4 & < & 6 \end{array}$$

11)
$$\begin{aligned} (-3) \times 4 + 6^2 \times (-3) + 5^2 &= \\ -3 \times 4 + 36 \times (-3) + 25 &= \\ -12 + (-108) + 25 &= -120 + 25 = -95 \end{aligned}$$

12)
$$\begin{aligned} 14 - 9 + 2^2 - (3 \div 6 \times 2^2) &= \\ (14 - 9 + 4) - (3 \div 6 \times 4) &= \\ 9 - (3/6 \times 4) &= 9 - (1/2 \times 4) = 9 - 2 = 7 \end{aligned}$$

13)
$$\begin{aligned} \frac{4}{3} \times \frac{6}{10} \div \frac{2}{3} &= \\ \frac{2 \cancel{A}}{\cancel{3}} \times \frac{\cancel{6} \cancel{B}^1}{\cancel{10}^5} \times \frac{3}{\cancel{2}^1} &= \frac{6}{5} = 1 \frac{1}{5} \end{aligned}$$

14)
$$\begin{array}{r} .17 \\ \underline{- .8} \\ \hline .136 \end{array}$$

(three decimal places in answer)

15)
$$(-8)(-7) = 56$$

16)
$$(-4)^2 = (-4)(-4) = 16$$

17)
$$2 = 2, 3 = 3, 4 = 2 \times 2, \text{ so LCM} = 2 \times 2 \times 3 = 12$$

$$\frac{6}{(12)} \frac{1}{2} + \frac{4}{(12)} \frac{2}{3} = \frac{3}{(12)} \frac{1}{4} X$$

(It is not necessary to write in "1" when dividing terms unless you wish.)

$$6 + 8 = 3X, \quad X = 4 \frac{2}{3}$$

18)
$$2, 5, 4 = 2 \times 2, \text{ so LCM} = 2 \times 2 \times 5 = 20$$

$$\frac{4}{(20)} \frac{3}{5} X + \frac{5}{(20)} \frac{3}{4} = \frac{10}{(20)} \frac{3}{2}$$

$$12X + 15 = 30, \quad X = 1 \frac{1}{4}$$

19)
$$3, 5, 9 = 3 \times 3, \text{ so LCM} = 3 \times 3 \times 5 = 45$$

$$\frac{5}{(45)} \frac{1}{9} X + \frac{15}{(45)} \frac{2}{3} = \frac{9}{(45)} \frac{1}{5}$$

$$5X + 30 = 9, \quad X = -4 \frac{1}{5}$$

20)
$$\begin{aligned} 4, 4 &= 2 \times 2, 8 = 2 \times 2 \times 2, \\ \text{so LCM} &= 2 \times 2 \times 2 \times 5 = 40 \end{aligned}$$

$$\frac{5}{(40)} \frac{3}{8} - \frac{8}{(40)} \frac{1}{5} X = \frac{10}{(40)} \frac{3}{4}$$

$$-8X = 15, \quad X = -1 \frac{7}{8}$$

3D

1)
$$\begin{aligned} Y - 3 &= 10 \\ Y - 3 + 3 &= 10 + 3 \\ Y &= 13 \end{aligned}$$

2)
$$\begin{aligned} 2B - 5 &= 13 \\ 2B &= 18 \\ 2B \div 2 &= 18 \div 2 \\ B &= 9 \end{aligned}$$

3)
$$\begin{aligned} 3C + 6 &= -9 \\ 3C &= -15 \\ 3C \div 3 &= -15 \div 3 \\ C &= -5 \end{aligned}$$

4)
$$\begin{aligned} 2D - 5 &= 1 \\ 2D &= 6 \\ 2D \div 2 &= 6 \div 2 \\ D &= 3 \end{aligned}$$

5)
$$\begin{aligned} 4E - 3 &= -3 \\ 4E &= 0 \\ E &= 0 \end{aligned}$$

6)
$$\begin{aligned} 3X + 8 &= -2X - 2 \\ 3X + 2X &= -2X + 2X - 10 \\ 5X &= -10 \\ 5X \div 5 &= -10 \div 5 \\ X &= -2 \end{aligned}$$

7)
$$\begin{aligned} 2Y - 2 &= 3Y - 6 \\ 2Y - 3Y &= -6 + 2 \\ -Y &= -4 \\ (-1)(-Y) &= (-1)(-4) \\ Y &= 4 \end{aligned}$$

8)
$$\begin{aligned} Z + 8 &= 2Z + 18 \\ Z - 2Z &= 18 - 8 \\ -Z &= 10 \\ Z &= -10 \end{aligned}$$

9)
$$\begin{array}{ccc} |3 \times 2 \times (-2)| & \textcircled{>} & 24 \div (-3) \\ |-12| & & -8 \\ 12 & > & -8 \end{array}$$

10)
$$\begin{array}{ccc} |17 - 3 - 20| & \textcircled{<} & |7 + 0 + 1| \\ |-6| & & |8| \\ 6 & < & 8 \end{array}$$

11)
$$\begin{aligned} [(6 - 2) \times 5^2 - 10] \div 5^2 &= \\ [4 \times 25 - 10] \div 25 &= \\ [100 - 10] \div 25 &= 90 \div 25 = 3 \frac{3}{5} \text{ or } 3.6 \end{aligned}$$

12)
$$\begin{aligned} (-7 - 6)^2 - (4 + 5 - 3)^2 &= \\ (-13)^2 - 6^2 &= 169 - 36 = 133 \end{aligned}$$

13)
$$\begin{aligned} \frac{5}{6} \times \frac{3}{7} \div \frac{2}{3} &= \\ \frac{5}{6} \times \frac{3}{7} \times \frac{3}{2} &= \frac{15}{28} \end{aligned}$$

14)
$$\begin{array}{r} 14. \\ 12 \sqrt{168} \\ \hline 12 \\ 48 \\ \hline 48 \end{array}$$

15)
$$2 = 2, 5 = 5, 10 = 2 \times 5, \text{ so LCM} = 2 \times 5 = 10$$

16)
$$\begin{aligned} \frac{2}{(10)} \frac{6}{8} X + \frac{1}{(10)} \frac{7}{10} &= \frac{5}{(10)} \frac{5}{2} X \\ 12X + 7 &= 25X, \quad X = 7/13 \end{aligned}$$

17)
$$\begin{aligned} 100 &= 10 \times 10, 1000 = 10 \times 10 \times 10 \\ \text{LCM} &= 10 \times 10 \times 10 = 1000 \end{aligned}$$

$$\begin{aligned} 1000(.83) + 1000(.04X) &= 1000(.325) \\ 830 + 40X &= 325 \\ 40X &= -505, \quad X = -12.625 \text{ or } -12 \frac{5}{8} \end{aligned}$$

18)
$$\begin{aligned} 10 &= 10, 100 = 10 \times 10 \\ \text{LCM} &= 10 \times 10 = 100 \\ 100(.18) + 100(.2X) &= 100(.17) \\ 18 + 20X &= 17 \\ 20X &= -1, \quad X = -.05 \text{ or } -1/20 \end{aligned}$$

19)
$$\begin{aligned} 10 &= 10, 100 = 10 \times 10 \\ \text{LCM} &= 10 \times 10 = 100 \\ 100(.8X) + 100(1.3) &= 100(7) + 100(.24) \\ 80X + 130 &= 700 + 24 \\ 80X &= 594, \quad X = 7.425 \text{ or } 7 \frac{17}{40} \end{aligned}$$

20)
$$\begin{aligned} 10 &= 10, 100 = 10 \times 10 \\ \text{LCM} &= 10 \times 10 = 100 \\ 100(8.2) - 100(4) &= 100(.08X) \\ 820 - 400 &= 8X \\ 420 = 8X, \quad X &= 52.5 \text{ or } 52 \frac{1}{2} \end{aligned}$$