

13. $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{3.5}{12.5} = \frac{7}{25}$
14. $\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{12}{12.5} = \frac{24}{25}$
15. $\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{3.5}{12} = \frac{7}{24}$
16. $\sin \alpha = \frac{\text{opp}}{\text{hyp}} = \frac{12}{12.5} = \frac{24}{25}$
17. $\cos \alpha = \frac{\text{adj}}{\text{hyp}} = \frac{3.5}{12.5} = \frac{7}{25}$
18. $\tan \alpha = \frac{\text{opp}}{\text{adj}} = \frac{12}{3.5} = \frac{24}{7}$
19. $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{4}{9}$
20. $\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{8.5}{9} = \frac{17}{18}$
21. $\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{4}{8.5} = \frac{8}{17}$
22. $\sin \alpha = \frac{\text{opp}}{\text{hyp}} = \frac{8.5}{9} = \frac{17}{18}$
23. $\cos \alpha = \frac{\text{adj}}{\text{hyp}} = \frac{4}{9}$
24. $\tan \alpha = \frac{\text{opp}}{\text{adj}} = \frac{8.5}{9} = \frac{17}{18}$

Lesson 1C

1. $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{8}{12.8} = \frac{80}{128} = \frac{5}{8}$
2. $\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{10}{12.8} = \frac{5}{6.4} = \frac{50}{64} = \frac{25}{32}$
3. $\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{8}{10} = \frac{4}{5}$
4. $\sin \alpha = \frac{\text{opp}}{\text{hyp}} = \frac{10}{12.8} = \frac{5}{6.4} = \frac{50}{64} = \frac{25}{32}$
5. $\cos \alpha = \frac{\text{adj}}{\text{hyp}} = \frac{8}{12.8} = \frac{80}{128} = \frac{5}{8}$
6. $\tan \alpha = \frac{\text{opp}}{\text{adj}} = \frac{10}{8} = \frac{5}{4}$
7. $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{12}{13.4} = \frac{120}{134} = \frac{60}{67}$
8. $\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{6}{13.4} = \frac{60}{134} = \frac{30}{67}$
9. $\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{12}{6} = 2$

10. $\sin \alpha = \frac{\text{opp}}{\text{hyp}} = \frac{6}{13.4} = \frac{60}{134} = \frac{30}{67}$
11. $\cos \alpha = \frac{\text{adj}}{\text{hyp}} = \frac{12}{13.4} = \frac{120}{134} = \frac{60}{67}$
12. $\tan \alpha = \frac{\text{opp}}{\text{adj}} = \frac{6}{12} = \frac{1}{2}$
13. $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{13.6}{15} = \frac{136}{150} = \frac{68}{75}$
14. $\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{6.4}{15} = \frac{64}{150} = \frac{32}{75}$
15. $\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{13.6}{6.4} = \frac{136}{64} = \frac{17}{8}$
16. $\sin \alpha = \frac{\text{opp}}{\text{hyp}} = \frac{6.4}{15} = \frac{64}{150} = \frac{32}{75}$
17. $\cos \alpha = \frac{\text{adj}}{\text{hyp}} = \frac{13.6}{15} = \frac{136}{150} = \frac{68}{75}$
18. $\tan \alpha = \frac{\text{opp}}{\text{adj}} = \frac{6.4}{13.6} = \frac{64}{136} = \frac{8}{17}$
19. $\sin \theta = \frac{\text{opp}}{\text{hyp}} = \frac{X}{2X} = \frac{1}{2}$
20. $\cos \theta = \frac{\text{adj}}{\text{hyp}} = \frac{X\sqrt{3}}{2X} = \frac{\sqrt{3}}{2}$
21. $\tan \theta = \frac{\text{opp}}{\text{adj}} = \frac{X}{X\sqrt{3}} = \frac{1}{\sqrt{3}} = \frac{\sqrt{3}}{3}$
22. $\sin \alpha = \frac{\text{opp}}{\text{hyp}} = \frac{X\sqrt{3}}{2X} = \frac{\sqrt{3}}{2}$
23. $\cos \alpha = \frac{\text{adj}}{\text{hyp}} = \frac{X}{2X} = \frac{1}{2}$
24. $\tan \alpha = \frac{\text{opp}}{\text{adj}} = \frac{X\sqrt{3}}{X} = \sqrt{3}$

Lesson 2A

1. $6^2 + 9^2 = H^2$
 $36 + 81 = H^2$
 $117 = H^2$
 $H \approx 10.82$
- $$\sin \theta = \frac{6}{10.82} \approx .5545$$
- $$\cos \theta = \frac{9}{10.82} \approx .8318$$
- $$\tan \theta = \frac{6}{9} \approx .6667$$
- $$\csc \theta = \frac{10.82}{6} \approx 1.8033$$
- $$\sec \theta = \frac{10.82}{9} \approx 1.2022$$
- $$\cot \theta = \frac{9}{6} \approx 1.5000$$

2.

$$\begin{aligned} 13^2 + 7^2 &= H^2 \\ 196 + 49 &= H^2 \\ 218 &= H^2 \\ H &= \sqrt{218} \\ H &\approx 14.76 \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{7}{14.76} \approx .4743 \\ \cos \theta &= \frac{13}{14.76} \approx .8808 \\ \tan \theta &= \frac{7}{13} \approx .5385 \\ \csc \theta &= \frac{14.76}{7} \approx 2.1086 \\ \sec \theta &= \frac{14.76}{13} \approx 1.1354 \\ \cot \theta &= \frac{13}{7} \approx 1.8571 \end{aligned}$$

5.

$$\begin{aligned} L^2 + 8^2 &= 20^2 \\ L^2 + 64 &= 400 \\ L^2 &= 400 - 64 \\ L^2 &= \sqrt{336} \\ L &\approx 18.33 \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{8}{20} = .4000 \\ \cos \theta &= \frac{18.33}{20} = .9165 \\ \tan \theta &= \frac{8}{18.33} \approx .4364 \\ \csc \theta &= \frac{20}{8} = 2.5000 \\ \sec \theta &= \frac{20}{18.33} \approx 1.0911 \\ \cot \theta &= \frac{18.33}{8} \approx 2.2913 \end{aligned}$$

3.

$$\begin{aligned} 7^2 + L^2 &= 9.9^2 \\ 49 + L^2 &= 98.01 \\ L^2 &= 98.01 - 49 \\ L^2 &= 49.01 \\ L &= \sqrt{49.01} \approx 7 \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{7}{9.9} \approx .7071 \\ \cos \theta &= \frac{7}{9.9} \approx .7071 \\ \tan \theta &= \frac{7}{7} \approx 1.0000 \\ \csc \theta &= \frac{9.9}{7} \approx 1.4143 \\ \sec \theta &= \frac{9.9}{7} \approx 1.4143 \\ \cot \theta &= \frac{7}{7} = 1.0000 \end{aligned}$$

6.

$$\begin{aligned} L^2 + 6.2^2 &= 14^2 \\ L^2 + 38.44 &= 196 \\ L^2 &= 196 - 38.44 \\ L^2 &= 157.56 \\ L &= \sqrt{157.56} \\ L &\approx 12.55 \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{12.55}{14} \approx .8964 \\ \cos \theta &= \frac{6.2}{14} \approx .4429 \\ \tan \theta &= \frac{12.55}{6.2} \approx 2.0242 \\ \csc \theta &= \frac{14}{12.55} \approx 1.1155 \\ \sec \theta &= \frac{14}{6.2} \approx 2.2581 \\ \cot \theta &= \frac{6.2}{12.55} \approx .4940 \end{aligned}$$

4.

$$\begin{aligned} 8^2 + L^2 &= 15^2 \\ 64 + L^2 &= 225 \\ L^2 &= 225 - 64 \\ L^2 &= 161 \\ L &= \sqrt{161} \\ L &\approx 12.69 \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{12.69}{15} \approx .8460 \\ \cos \theta &= \frac{8}{15} \approx .5333 \\ \tan \theta &= \frac{12.69}{8} \approx 1.5863 \\ \csc \theta &= \frac{15}{12.69} \approx 1.1820 \\ \sec \theta &= \frac{15}{8} = 1.8750 \\ \cot \theta &= \frac{8}{12.69} \approx .6304 \end{aligned}$$

Lesson 2B

1.

$$\begin{aligned} 4.5^2 + 6.6^2 &= H^2 \\ 20.25 + 43.56 &= H^2 \\ 63.81 &= H^2 \\ \sqrt{63.81} &= H \\ H &\approx 7.99 \end{aligned}$$

$$\begin{aligned} \sin \theta &= \frac{4.5}{7.99} \approx .5632 \\ \cos \theta &= \frac{6.6}{7.99} \approx .8260 \\ \tan \theta &= \frac{4.5}{6.6} \approx .6818 \\ \csc \theta &= \frac{7.99}{4.5} \approx 1.7756 \\ \sec \theta &= \frac{7.99}{6.6} \approx 1.2106 \\ \cot \theta &= \frac{6.6}{4.5} \approx 1.4667 \end{aligned}$$

2.

$$L^2 + 6.8^2 = \sqrt{51}^2$$

$$L^2 + 46.24 = 51$$

$$L^2 = 51 - 46.24$$

$$L^2 = 4.76$$

$$L = \sqrt{4.76}$$

$$L \approx 2.18$$

$$\sqrt{51} \approx 7.14$$

$$\sin \theta = \frac{2.18}{7.14} \approx .3053$$

$$\cos \theta = \frac{6.8}{7.14} \approx .9524$$

$$\tan \theta = \frac{2.18}{6.8} \approx .3206$$

$$\csc \theta = \frac{7.14}{2.18} \approx 3.2752$$

$$\sec \theta = \frac{7.14}{6.8} = 1.0500$$

$$\cot \theta = \frac{6.8}{2.18} \approx 3.1193$$

3. $10^2 + \sqrt{3}^2 = H^2$

$$100 + 3 = H^2$$

$$103 = H^2$$

$$\sqrt{103} = H$$

$$H \approx 10.15$$

$$\sqrt{3} \approx 1.73$$

$$\sin \theta = \frac{1.73}{10.15} \approx .1704$$

$$\cos \theta = \frac{10}{10.15} \approx .9852$$

$$\tan \theta = \frac{1.73}{10} = .1730$$

$$\csc \theta = \frac{10.15}{1.73} \approx 5.8671$$

$$\sec \theta = \frac{10.15}{10} = 1.0150$$

$$\cot \theta = \frac{10}{1.73} \approx 5.7803$$

4.

$$(7\sqrt{2})^2 + (7\sqrt{3})^2 = H^2$$

$$(7)(7)\sqrt{2}\sqrt{2} + (7)(7)\sqrt{3}\sqrt{3} = H^2$$

$$(49)(2) + (49)(3) = H^2$$

$$98 + 147 = H^2$$

$$245 = H^2$$

$$H \approx 15.65$$

$$7\sqrt{2} \approx 9.9$$

$$7\sqrt{3} \approx 12.12$$

$$\sin \theta = \frac{9.9}{15.65} \approx .6326$$

$$\cos \theta = \frac{12.12}{15.65} \approx .7744$$

$$\tan \theta = \frac{9.9}{12.12} \approx .8168$$

$$\csc \theta = \frac{15.65}{9.9} \approx 1.5808$$

$$\sec \theta = \frac{15.65}{12.12} \approx 1.2913$$

$$\cot \theta = \frac{12.12}{9.9} \approx 1.2242$$

5. $(2\sqrt{3})^2 + 11^2 = H^2$

$$(2)(2)\sqrt{3}\sqrt{3} + 121 = H^2$$

$$4(3) + 121 = H^2$$

$$133 = H^2$$

$$H \approx 11.53$$

$$2\sqrt{3} \approx 3.46$$

$$\sin \theta = \frac{3.46}{11.53} \approx .3001$$

$$\cos \theta = \frac{11}{11.53} \approx .9540$$

$$\tan \theta = \frac{3.46}{11} \approx .3145$$

$$\csc \theta = \frac{11.53}{3.46} \approx 3.3324$$

$$\sec \theta = \frac{11.53}{11} \approx 1.0482$$

$$\cot \theta = \frac{11}{3.46} \approx 3.1792$$

6. $5^2 + 12^2 = H^2$

$$25 + 144 = H^2$$

$$169 = H^2$$

$$\sqrt{169} = H^2$$

$$H = 13$$

$$\sin \theta = \frac{5}{13} \approx .3846$$

$$\cos \theta = \frac{12}{13} \approx .9231$$

$$\tan \theta = \frac{5}{12} \approx .4167$$

$$\csc \theta = \frac{13}{5} = 2.6000$$

$$\sec \theta = \frac{13}{12} \approx 1.0833$$

$$\cot \theta = \frac{12}{5} = 2.4000$$

Lesson 2C

1. $9^2 + 8^2 = H^2$

$$81 + 64 = H^2$$

$$145 = H^2$$

$$\sqrt{145} = H^2$$

$$H \approx 12.04$$

$$\sin \theta = \frac{8}{12.04} \approx .6645$$

$$\cos \theta = \frac{9}{12.04} \approx .7475$$

$$\tan \theta = \frac{8}{9} \approx .8889$$

$$\csc \theta = \frac{12.04}{8} \approx 1.5050$$

$$\sec \theta = \frac{12.04}{9} \approx 1.3378$$

$$\cot \theta = \frac{9}{8} = 1.1250$$

$$\begin{aligned}
 2. \quad & 5^2 + 5^2 = H^2 & \sin \theta &= \frac{5}{7.07} \approx .7072 \\
 & 25 + 25 = H^2 & \cos \theta &= \frac{5}{7.07} \approx .7072 \\
 & 50 = H^2 & \tan \theta &= \frac{5}{5} = 1.0000 \\
 & \sqrt{50} = H & \csc \theta &= \frac{7.07}{5} = 1.4140 \\
 & H \approx 7.07 & \sec \theta &= \frac{7.07}{5} = 1.4140 \\
 & & \cot \theta &= \frac{5}{5} = 1.0000
 \end{aligned}$$

$$\begin{aligned}
 3. \quad & 3^2 + 3^2 = H^2 & \sin \theta &= \frac{3}{4.24} \approx .7075 \\
 & 9 + 9 = H^2 & \cos \theta &= \frac{3}{4.24} \approx .7075 \\
 & 18 = H^2 & \tan \theta &= \frac{3}{3} = 1.0000 \\
 & \sqrt{18} = H & \csc \theta &= \frac{4.24}{3} \approx 1.4133 \\
 & H \approx 4.24 & \sec \theta &= \frac{4.24}{3} \approx 1.4133 \\
 & & \cot \theta &= \frac{3}{3} = 1.0000
 \end{aligned}$$

$$\begin{aligned}
 4. \quad & 12^2 + L^2 = 13^2 & \sin \theta &= \frac{5}{13} \approx .3846 \\
 & 144 + L^2 = 169 & \cos \theta &= \frac{12}{13} \approx .9231 \\
 & L^2 = 169 - 144 & \tan \theta &= \frac{5}{12} \approx .4167 \\
 & L^2 = 25 & \csc \theta &= \frac{13}{5} = 2.6000 \\
 & L = \sqrt{25} & \sec \theta &= \frac{13}{12} \approx 1.0833 \\
 & L = 5 & \cot \theta &= \frac{12}{5} = 2.4000
 \end{aligned}$$

$$\begin{aligned}
 5. \quad & 4^2 + 6^2 = H^2 & \sin \theta &= \frac{6}{7.21} \approx .8322 \\
 & 16 + 36 = H^2 & \cos \theta &= \frac{4}{7.21} \approx .5548 \\
 & 52 = H^2 & \tan \theta &= \frac{6}{4} = 1.5000 \\
 & \sqrt{52} = H & \csc \theta &= \frac{7.21}{6} \approx 1.2017 \\
 & H \approx 7.21 & \sec \theta &= \frac{7.21}{4} = 1.8025 \\
 & & \cot \theta &= \frac{4}{6} \approx .6667
 \end{aligned}$$

$$\begin{aligned}
 6. \quad & 7^2 + 7^2 = H^2 & \sin \theta &= \frac{7}{9.9} \approx .7071 \\
 & 49 + 49 = H^2 & \cos \theta &= \frac{7}{9.9} \approx .7071 \\
 & 98 = H^2 & \tan \theta &= \frac{7}{7} = 1.0000 \\
 & \sqrt{98} = H & \csc \theta &= \frac{9.9}{7} \approx 1.4143 \\
 & H \approx 9.90 & \sec \theta &= \frac{9.9}{7} \approx 1.4143 \\
 & & \cot \theta &= \frac{7}{7} = 1.0000
 \end{aligned}$$

Lesson 3A

1. $\cos 37^\circ = .7986$
2. $\tan 51^\circ = 1.2349$
3. $\sin 20^\circ = .3420$
4. $\sin 49^\circ = .7547$
5. $\cos 65^\circ = .4226$
6. $.6249 = \tan 32^\circ$
7. $.4540 = \cos 63^\circ$
8. $.0875 = \tan 5^\circ$
9. $.9781 = \sin 78^\circ$
10. $14.3007 = \tan 86^\circ$
11. $\sin \theta = \frac{20}{26.9} \approx .7435$
 $\cos \theta = \frac{18}{26.9} \approx .6691$
 $\tan \theta = \frac{20}{18} \approx 1.1111$
 $\theta = 48^\circ$
 $\sin \alpha = \frac{18}{26.9} \approx .6691$
 $\cos \alpha = \frac{20}{26.9} \approx .7435$
 $\tan \alpha = \frac{18}{20} = .9000$
 $\alpha = 42^\circ$