(2) COMBINE.
$$\frac{y}{z} + \frac{y}{x} + \frac{3y}{x+2}$$

Ch. 3 - Scientific Notation/Combining Like Terms

SCIENTIFIC NOTATION

A. AA x 10B

TRY ON CALCULATOR IN SCIENTIFIC NOTATION



NOW TRY ON CALCULATOR

Combine Like TERMS (SIMPLIFY FIRST)
$$0 \frac{30x^{-1}}{10} + 2^2y^2 - \frac{2}{x} + \frac{2Y}{y-1}$$

②
$$3xy^2 - 4x^2y^2 + \frac{7x^2}{xy^2}$$

Lesson 3 Scientific Notation and Combining Like Terms

Scientific notation is used in science to solve equations with very large and/or very small numbers. If we were asked to compute 200 times the distance from the earth to the sun (which is 93 million miles, or 93,000,000), using the normal method of multiplying, it would require a good deal of paper and pencil, and have lots of zeroes.

Scientific notation provides an easier and more efficient method.

It is closely related to exponential notation.

93,000,000 in exponential notation is $9 \times 10^7 + 3 \times 10^6$. In scientific notation you keep the 9 and the 3 together, instead of separating them, and place the decimal point so the 9 is in the units place. Then choose the exponent figured from the number in the units place. The 3 is forgotten when choosing the exponent.

Example 1 Multiply 93,000,000 times 200.

93,000,000 in scientific notation is 9.3 x 10⁷

200 in scientific notation is 2 x 10²

To solve our original problem of 200 times the distance from the sun to the earth, multiply the numbers times the numbers & the exponents times the exponents.

$$(9.3 \times 10^7)(2 \times 10^2) = (9.3 \times 2)(10^7 \times 10^2) = (18.6)(10^9) = (1.86 \times 10^1)(10^9) = 1.86 \times 10^{10}$$

Example 2 Multiply 1,900 x 50.

 $1,900 = 1.9 \times 10^3$ in scientific notation

50 in scientific notation is 5 x 101

Multiply the numbers times the numbers & the exponential terms times the exponential terms.

$$(1.9 \times 10^3)(5 \times 10^1) = (1.9 \times 5)(10^3 \times 10^1) = (9.5)(10^4)$$

You can also show very small decimal numbers with scientific notation. Remember that you may only have one number in the units place and the rest as decimals. Study the examples:

Example 3 Change .000054 to Scientific Notation

$$0.000054 = 5.4 \times 10^{-5} = 5.4 \times \frac{1}{105}$$
 or $5.4 \times \frac{1}{100,000}$

Example 4 Multiply 30,000,000 x .000023.

 $30,000,000 = 3.0 \times 10^7$ in scientific notation

.000023 in scientific notation is 2.3 x 10-5

$$(3 \times 10^{7})(2.3 \times 10^{-5}) = (3 \times 2.3)(10^{7} \times 10^{-5}) = (6.9)(10^{2}) = 6.9 \times 10^{2}$$

Example 5 Divide 500,000 ÷ 8,000

 $500,000 = 5.0 \times 10^5$ in scientific notation

8,000 in scientific notation is 8.0 x 103

$$(5 \times 10^{5}) \div (8 \times 10^{3}) = (5 \div 8)(10^{5} \div 10^{3}) = (.625)(10^{2}) = (6.25 \times 10^{-1}) \times 10^{2} = 6.25 \times 10^{1}$$

Practice Problems

- 1) 93,000,000 x .000054 =
- 2) $18,000 \times .007 =$
- 3) $640,000 \times .92 =$
- 4) 12,400 ÷ .04 =
- 5) $40,000 \times 3,000 \div 60 =$
- 6) .00058 x .0023 =

Even though to be in the proper form, the digit must be in the units place, there are times when doing larger problems that it is advantageous to leave the numbers larger, and make the necessary corrections in the exponents. This allows for reducing or dividing by a common factor (sometimes called cancelling), and saves steps in problem solving. Example 6 employs this technique. You can do the long method to compare the results if you wish.

Example 6

$$\frac{(2,700)(3,500)}{(9,000,000)} = \frac{(27 \times 10^{2})(35 \times 10^{2})}{(90 \times 10^{5})}$$

$$\frac{3}{(27 \times 10^{2})(35 \times 10^{2})}$$

$$\frac{(90 \times 10^{5})}{10}$$
You can divide 27 and 90 by 9.

$$\frac{(27 \times 10^{2})(35 \times 10^{2})}{(27 \times 10^{2})(95 \times 10^{2})}$$
Then you can divide 35 and 10 by 5.

$$\frac{(3 \times 10^{2})(7 \times 10^{2})}{(2 \times 10^{5})} = \frac{(3 \times 7)(10^{2} \times 10^{2})}{(2 \times 10^{5})} = (21)(10^{4}) \div (2 \times 10^{5})$$

$$= (21 \div 2)(10^{4-5})$$

$$= (10.5)(10^{-1}) = (1.05 \times 10^{1})(10^{-1})$$

$$= 1.05$$

Combining Like Terms One of the key concepts we have focused on since the beginning is that numbers tell us now many, and place value tells what kind or what value. Building on this, we found that you can only combine or compare things that are the same kind, or value.

The terms and expressions in Algebra 2 are becoming more complex, but the concepts remain the same. What we need to learn in this lesson is how to identify which terms are the same kind, then combine them. The strategies to be employed are not new either. When the terms are rational expressions, the first step is to reduce or simplify as much as possible. When exponents are present, either make them all positive, or put all on the same line by changing the signs of the exponent (opposite sign, opposite place). Some of the problems look tricky, but after patiently applying these strategies, we can distinguish between the apples and the oranges and combine the apples with the apples and the oranges with the oranges. Let's do a few examples.

Example 1

$$\frac{30X^{-1}}{10} + 2^{2}Y^{2} - \frac{2}{X} + \frac{2Y}{Y^{-1}}$$

$$3X^{-1} + 4Y^{2} - \frac{2}{X} + \frac{2Y}{Y^{-1}}$$

$$\frac{3}{X}$$
 + 4Y2 - $\frac{2}{X}$ + 2Y² = $\frac{1}{X}$ + 6Y²

$$3X^{-1} + 4Y^2 - 2X^{-1} + 2Y^2 = X^{-1} + 6Y^2$$

Step #1 - Simplify what you can.

Step #2 - Make all exponents positive, or

put all the variables on one line.

Example 2

$$3XY^{-2} - 4X^{2}Y^{2} + \frac{7X^{2}}{XY^{2}}$$

$$3XY^{-2} - 4X^{2}Y^{2} + \frac{7X}{Y^{2}}$$

$$\frac{3X}{Y^2} - 4X^2Y^2 + \frac{7X}{Y^2} = \frac{10X}{Y^2} - 4X^2Y^2$$

$$3XY^{-2} - 4X^{2}Y^{2} + 7XY^{-2} = 10XY^{-2} - 4X^{2}Y^{2}$$

Step #1 - Simplify what you can.

Step #2 - Make all exponents positive, or

put all the variables on one line.

Practice Problems Simplify and combine like terms.

1)
$$\frac{5B-1}{A-1} - \frac{7B^2A^2}{B^3A^1} + \frac{3B^3B^0}{A^1A^{-2}} =$$

2)
$$\frac{5X^4X^{-1}}{X^2Y^2}$$
 - 2X2Y-2 + $\frac{6X^4Y^2X^{-1}}{XY^4}$ = 3) 8XXY - YXXY + $\frac{2XY}{X^{-1}}$ =

3)
$$8XXY - YXXY + \frac{2XY}{x-1} = \frac{1}{x}$$

4)
$$4X^2X^{-1} - \frac{12X^2}{x^3} + 8X =$$

5)
$$6A^2B^{-2}A - \frac{4AB^2B^{-1}}{A^{-1}B^3} + \frac{9B^3B^{-3}}{A^{-3}AB^2} = 6$$
 6) $9X^{-2}A^{-2}X + X^3AA^{-1} + \frac{7A^3X^0}{A^2X^3}$

6)
$$9X^{-2}A^{-2}X + X^3AA^{-1} + \frac{7A^3X^0}{A^2X^3}$$

3H

Significant digits

Scientific notation is often used when working with very large or very small measurements. An important concept to remember is the fact that measurements are always approximate. Therefore, it is important to use the correct number of significant digits in your answer. Review the following information.

(There is a lesson on this in Algebra 1.)

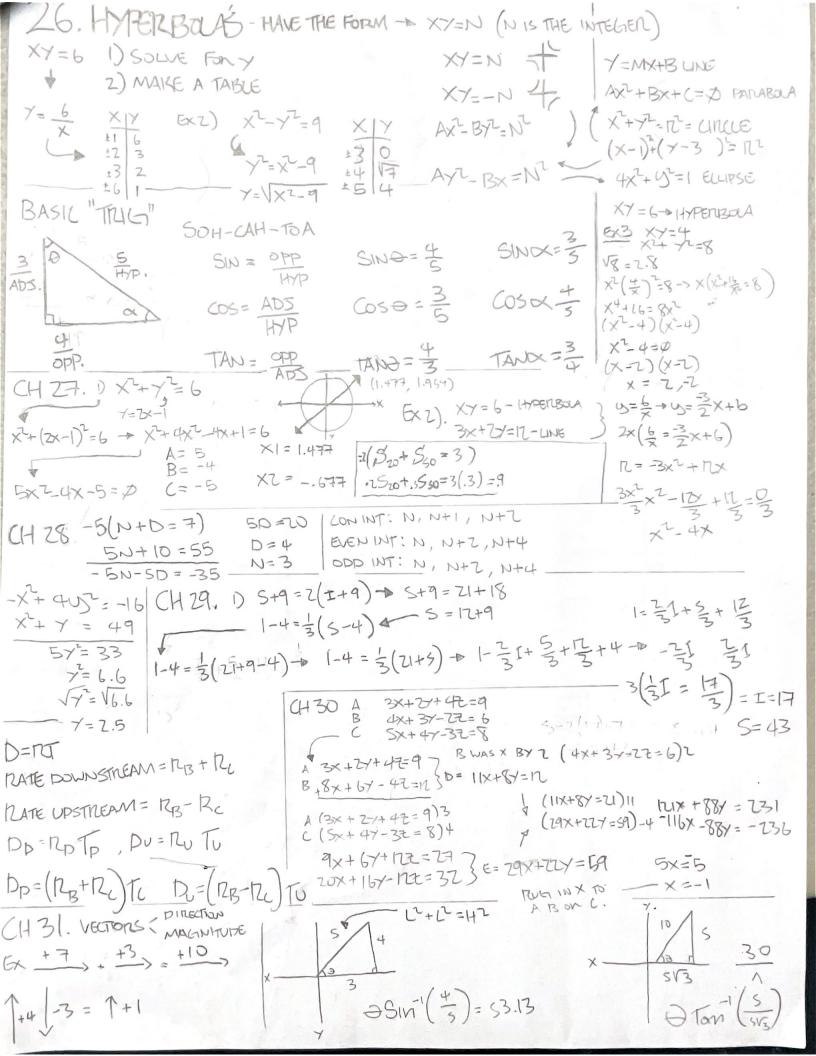
All digits except zero are always counted as significant digits. The number 25 has two significant digits, 31.4 has three significant digits, and .456 also has three significant digits.

Zero may or may not be a significant digit, depending on its position. The number 6,007 has four significant digits because it represents a measure that is accurate to the nearest unit. The number 6,700 has only two significant digits and two place holders, because it may have been rounded to the nearest hundred.

The number .006 has one significant digit and two zeros that are merely place holders. However 6.0 and .60 both have two significant digits because the zeros have been added to show that the measurement is accurate to a certain place value.

The next page has problems to practice this skill.

AMEND



HONORS LESSON 3H

Tell how many significant digits are in each of the following measurements.

2. 13,456 ft

3. 2,000 m

4. 1,608 in

5. .59 cm

6. .068 km

7. 1.3 mi

8. .400 m

9. 3.000 ft

There are special terms used to name the parts of a number written in scientific notation. The first part of the expression is the *mantissa* and the exponent is the *characteristic*. An example is 2.45×10^3 . The mantissa is 2.45, and the characteristic is 3. Look at the mantissa of a number written in scientific notation to determine how many significant digits that number has.

Write each measurement in scientific notion and tell how many significant digits it has. The next honors page will tell you how to use significant digits in computations.

10. 245,000,000 ft

11. .00009 m

12. 1,304 tons

13. 1.50 g