

10A

1) 7 terms

$$1A^{670} + 6A^{571} + 15A^{472} + 20A^{373} + 15A^{274} + 6A^{175} + 1A^{076}$$

$$A^6 + 42A^5 + 735A^4 + 6860A^3 + 36,015A^2 + 100,842A + 117,649$$

2) 6 terms

$$1X^5(-2)^0 + 5X^4(-2)^1 + 10X^3(-2)^2 + 10X^2(-2)^3 + 5X^1(-2)^4 + 1X^0(-2)^5$$

$$X^5 - 10X^4 + 40X^3 - 80X^2 + 80X - 32$$

3) 5 terms

$$1(3X)^{410} + 4(3X)^{311} + 6(3X)^{212} + 4(3X)^{113} + 1(3X)^{014}$$

$$81X^4 + 108X^3 + 54X^2 + 12X + 1$$

4) 7 terms

$$1R^6(-1/2)^0 + 6R^5(-1/2)^1 + 15R^4(-1/2)^2 + 20R^3(-1/2)^3 + 15R^2(-1/2)^4 + 6R^1(-1/2)^5 + 1R^0(-1/2)^6$$

$$R^6 - 3R^5 + 15/4 R^4 - 5/2 R^3 + 15/16 R^2 - 3/16 R + 1/64$$

$$5) \frac{5 \cdot A \cdot B}{1 \cdot Z \cdot B} = 10 \quad 10A^2(2B)^3 = 80A^2B^3$$

$$6) \frac{3 \cdot B \cdot 5}{1 \cdot Z} = 15 \quad 15X^42^2 = 60X^4$$

$$7) \frac{7 \cdot B \cdot 5 \cdot A}{1 \cdot Z \cdot B \cdot A} = 35 \quad 35(2X)^3(-2)^4 = 4,480X^3$$

$$8) \frac{4}{1} = 4 \quad 4X^3(-1/3)^1 = -4/3 X^3$$

$$9) \frac{2 \cdot 5 \cdot 2 \cdot A}{1 \cdot Z \cdot B} = 20 \quad 20X^3Y^3$$

$$10) \frac{4 \cdot 7 \cdot 2 \cdot B \cdot A}{1 \cdot Z \cdot B \cdot X \cdot B} = 56 \quad 56P^3(-Q)^5 = -56P^3Q^5$$

10B

1) 4 terms

$$1B^{340} + 3B^{241} + 3B^{142} + 1B^{043}$$

$$B^3 + 12B^2 + 48B + 64$$

2) 7 terms

$$1(2X)^{610} + 6(2X)^{511} + 15(2X)^{412} + 20(2X)^{313} + 15(2X)^{214} + 6(2X)^{115} + 1(2X)^{016}$$

$$64X^6 + 192X^5 + 240X^4 + 160X^3 + 60X^2 + 12X + 1$$

3) 6 terms

$$1R^5(-T)^0 + 5R^4(-T)^1 + 10R^3(-T)^2 + 10R^2(-T)^3 + 5R^1(-T)^4 + 1R^0(-T)^5$$

$$R^5 - 5R^4T + 10R^3T^2 - 10R^2T^3 + 5RT^4 - T^5$$

4) 5 terms

$$1(1/2 X)^4(1/2 Y)^0 + 4(1/2 X)^3(1/2 Y)^1 + 6(1/2 X)^2(1/2 Y)^2 + 4(1/2 X)^1(1/2 Y)^3 + 1(1/2 X)^0(1/2 Y)^4$$

$$1/16 X^4 + 1/4 X^3Y + 3/8 X^2Y^2 + 1/4 XY^3 + 1/16 Y^4$$

$$5) 1X^{10}(2Y)^0 = X^{10}$$

$$6) \frac{B \cdot B \cdot A \cdot B \cdot C \cdot 1}{1 \cdot Z \cdot B \cdot A \cdot B \cdot B} = 1 \quad 1A^0B^6 = B^6$$

$$7) \frac{2 \cdot 3}{1 \cdot Z} = 6 \quad 6(2X)^23^2 = 216X^2$$

$$8) \frac{3 \cdot 5 \cdot A \cdot B}{1 \cdot Z \cdot B \cdot A} = 15 \quad 15Q^2(2/3)^4 = 80/27 Q^2$$

$$9) \frac{5}{1} = 5 \quad 5(3R)^4(-T)^1 = -405R^4T$$

$$10) \frac{4 \cdot B \cdot Z}{1 \cdot Z \cdot B} = 4 \quad 4(2X)^1(-2Y)^3 = -64XY^3$$

10C

1) 6

2) $X^5 + X^4 + 10X^3 + 32 + 10X^2 + 33 + 5X^4 + 1 + X^0 + 35$
 $X^5 + 15X^4 + 90X^3 + 270X^2 + 405X + 243$

3) 7

4) $1X^6 + (-4)^0 + 6X^5 + (-4)^1 + 15X^4 + (-4)^2 + 20X^3 + (-4)^3 +$
 $15X^2 + (-4)^4 + 6X + (-4)^5 + (-4)^6$
 $X^6 - 24X^5 + 240X^4 - 1280X^3 + 3840X^2 - 6144X + 4096$

5) $4(2X)^1 Y^3 = 8XY^3$

6) $4(2X)^3 Y = 32X^3 Y$

7) $15(X)^4(-2)^2 = 60X^4$

8) $15(X)^2(-2)^4 = 240X^2$

9) $X^2 + 6AX + 9A^2$

10) $(3X - 7)^2$

11) $X^3 + 3X^2(12) + 3X(12^2) + 12^3$
 $X^3 + 36X^2 + 432X + 1728$

12) $(2X)^3 + 3(2X)^2(-1/3) + 3(2X)(-1/3)^2 + (-1/3)^3$
 $8X^3 - 4X^2 + 2/3X - 1/27$

13) $\frac{(2\sqrt{2} + 1)(3\sqrt{3} + 1)}{(3\sqrt{3} - 1)(3\sqrt{3} + 1)} =$

2) $\frac{6\sqrt{5} + 2\sqrt{2} + 3\sqrt{3} + 1}{9 \cdot 3 - 1} =$
 $\frac{6\sqrt{6} + 2\sqrt{2} + 3\sqrt{3} + 1}{26}$

14) $\frac{-8i}{4 + 5i} \cdot \frac{(4 - 5i)}{(4 - 5i)} = \frac{-32i + 40i^2}{16 - 25i^2} = \frac{-32i - 40}{41}$

15) $(-616)(i^3) = (-616)(i^2)(i) = 616i$

16) $(-12)(\sqrt{-36}) = -12(\sqrt{36}\sqrt{-1}) =$
 $-12 \cdot 6 \cdot i = -72i$

17) $6\sqrt{\frac{1}{2}} - \frac{9\sqrt{8}}{2} =$

$\frac{6\sqrt{1}\sqrt{2}}{\sqrt{2}\sqrt{2}} - \frac{9\sqrt{4}\sqrt{2}}{2} =$

$\frac{6\sqrt{2}}{2} - \frac{18\sqrt{2}}{2} = -6\sqrt{2}$

18) $(4)^{5/2} = 32$

19) $\frac{2X^2 - 3X - 2}{X^3 - 2X^2} \div \frac{4X^2 - 12X}{X^2 - 5X + 6} =$
 $\frac{(2X + 1)(X - 2)}{X^2(X - 2)} \cdot \frac{(X - 3)(X - 2)}{4X(X - 3)} =$

$\frac{2X^2 - 3X - 2}{4X^3}$

20) $\frac{10X}{Y} - \frac{Y}{4X} - \frac{2Y(4)}{X(4)} = \frac{10X}{Y} - \frac{9Y}{4X}$

10D

1) 6

13) $\frac{(8\sqrt{11} - 6)(4\sqrt{2} - 3)}{(4\sqrt{2} + 3)(4\sqrt{2} - 3)} =$

2) $X^5 + 5X^4A + 10X^3A^2 + 10X^2A^3 + 5XA^4 + A^5$

$\frac{32\sqrt{22} - 24\sqrt{11} - 24\sqrt{2} + 18}{16 \cdot 2 \cdot 9} =$

3) 5

4) $(1/3X)^4 + 4(1/3X)^32 + 6(1/3X)^22^2 + 4(1/3X)^23 + 2^4$
 $1/81X^4 + 8/27X^3 + 8/3X^2 + 32/3X + 16$

14) $\frac{2i}{(1+9i)(1-9i)} = \frac{21-18i^2}{1-81i^2} = \frac{2i+18}{82} =$
 $\frac{i+9}{41}$

5) $\frac{6 \cdot 5 \cdot 4}{1 \cdot 2 \cdot 3} X^3(-2/3)^3 = -160/27 X^3$

15) $540i^2 = -540$

6) $\frac{6}{1} X^5(-2/3) = -4X^5$

16) $(72)(-7) = -504$

17) $\sqrt{\frac{5}{8}} - 2\sqrt{160} =$

$\frac{\sqrt{5}\sqrt{2}}{\sqrt{8}\sqrt{2}} - 2\sqrt{16}\sqrt{10} = \frac{\sqrt{10}}{4} - 8\sqrt{10}$

$\frac{\sqrt{10}}{4} - \frac{32\sqrt{10}}{4} = \frac{-31\sqrt{10}}{4}$

8) $\frac{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{1 \cdot 2 \cdot 3 \cdot 4 \cdot 5} X^0(-3)^5 = -243$

18) $(5)^3 = 125$ or

$[(125)^{1/3}]^3 = 125^1 = 125$

10) $(4X - 3)^2$

19) $\frac{4X^2 - 1}{2X + 1} \div \frac{4X^2 - 4X + 1}{8X} =$

$\frac{(2X-1)(2X+1)}{(2X+1)} \cdot \frac{8X}{(2X-1)(2X-1)} =$

$\frac{8X}{2X-1}$

11) $X^3 + 3X^2(-10) + 3X(-10)^2 + (-10)^3$
 $X^3 - 30X^2 + 300X - 1000$

12) $X^3 + 3X^2(1/2) + 3(X)(1/2)^2 + (1/2)^3$
 $X^3 + 3/2X^2 + 3/4X + 1/8$

20) $4X + 6Y + 9XY^5$

10E

1) 6

2) $X^5 + 5X^4(-4) + 10X^3(-4)^2 + 10X^2(-4)^3 + 5X(-4)^4 + (-4)^5$
 $X^5 - 20X^4 + 160X^3 - 640X^2 + 1280X - 1,024$

3) 5

4) $X^4 + 4X^32 + 6X^{22} + 4X^{23} + 24$
 $X^4 + 8X^3 + 24X^2 + 32X + 16$

5) $\frac{5}{1} \cdot \frac{4 \cdot 3}{2 \cdot 3} (2X)^2 3^3 = (10)4X^2(27) = 1080X^2$

6) $\frac{5}{1} (2X)^4 3^1 = (5)16X^4(3) = 240X^4$

7) $(2X)^4 = 16X^4$

8) $\frac{4 \cdot 3}{1 \cdot 2} (2X)^2 1^2 = (6)4X^2(1) = 24X^2$

9) $X^2 + 2XA + A^2$

10) $(6X - 1/2)^2$

11) $X^3 + 3X^2(4/5) + 3X(4/5)^2 + (4/5)^3$
 $X^3 + 12/5 X^2 + 48/25 X + 64/125$

12) $(3X)^3 + 3(3X)^2 + 3(3X) + 1^3$
 $27X^3 + 27X^2 + 9X + 1$

13) $\frac{\sqrt{8}(5\sqrt{7} + 4)}{(5\sqrt{7} - 4)(5\sqrt{7} + 4)} =$

$$\frac{5\sqrt{56} + 4\sqrt{8}}{25 \cdot 7 - 16} =$$

$$\frac{5\sqrt{4} \sqrt{14} + 4\sqrt{4} \sqrt{2}}{159} = \frac{10\sqrt{14} + 8\sqrt{2}}{159}$$

14) $\frac{-3i(2+11i)}{(2-11i)(2+11i)} = \frac{-6-33i^2}{4-121i^2} =$

$$\frac{-6i+33}{125}$$

15) $-30i$

16) $(-35)(-\sqrt{16}) = -35 \cdot -4 = 140$

17) $\sqrt{\frac{1}{10}} + 3\sqrt{90} =$

$$\frac{\sqrt{1}\sqrt{10}}{\sqrt{10}\sqrt{10}} + \frac{3\sqrt{90}(10)}{(10)} = \frac{\sqrt{10}}{10} + \frac{30\sqrt{90}}{10} =$$

$$\frac{\sqrt{10}}{10} + \frac{30\sqrt{5}\sqrt{10}}{10} = \frac{\sqrt{10} + 90\sqrt{10}}{10} =$$

$$\frac{91\sqrt{10}}{10}$$

18) $(9)^{3/2} = 27$

19) $\frac{(X+2)(X+3)}{(X-4)(X+4)} \cdot \frac{(X+2)(X+4)}{(X+3)(X+3)} =$

$$\frac{X^2 + 4X + 4}{X^2 - X - 12}$$

20) $12X^4Y^5 + \frac{10X^4}{Y^5} + 8X^4Y^5 =$

$$\frac{10X^4}{Y^5} + 20X^4Y^5$$

11A

1) 25

2) 16

3) $4X$

4) $30A$

5) $X^2 + 2X + 1 = -3 + 1$
 $(X + 1)^2 = -2$
 $X + 1 = \pm\sqrt{-2}$
 $X = -1 \pm i\sqrt{2}$

6) $X^2 - 5X + 4 = 0$
 $(X - 4)(X - 1) = 0$
 $X - 4 = 0 \quad X - 1 = 0$
 $X = 4 \quad X = 1$

7) $2(X^2 + 4X + 1) = 0$
 $X^2 + 4X + 4 = -1 + 4$
 $(X + 2)^2 = 3$
 $X + 2 = \pm\sqrt{3}$
 $X = -2 \pm \sqrt{3}$

8) $X^2 + 4X + 4 = 7 + 4$
 $(X + 2)^2 = 11$
 $X + 2 = \pm\sqrt{11}$
 $X = -2 \pm \sqrt{11}$

9) $3(X^2 - 3X + 1) = 0$
 $X^2 - 3X + \frac{9}{4} = -1 + \frac{9}{4}$
 $(X - \frac{3}{2})^2 = \frac{5}{4}$
 $X - \frac{3}{2} = \pm\frac{\sqrt{5}}{2}$
 $X = \frac{3}{2} \pm \frac{\sqrt{5}}{2} \text{ or } \frac{3 \pm \sqrt{5}}{2}$

10) $X^2 - 2X + 1 = 11 + 1$
 $(X - 1)^2 = 12$
 $X - 1 = \sqrt{12}$
 $X = 1 \pm 2\sqrt{3}$

For most problems, the check for only one solution is shown.
The check for the other solution should be similar.

$$(-1 + i\sqrt{2})^2 + 2(-1 + i\sqrt{2}) + 3 = 0$$

~~$$1 - 2i\sqrt{2} - 2 - 2 + 2i\sqrt{2} + 3 = 0$$~~

$$1 - 2 - 2 + 3 = 0$$

$$(4)^2 - 5(4) + 4 = 0$$

$$16 - 20 + 4 = 0$$

$$(1)^2 - 5(1) + 4 = 0$$

$$1 - 5 + 4 = 0$$

$$[2(-2 + \sqrt{3})^2 + 8(-2 + \sqrt{3}) + 2 = 0] \div 2$$

$$(-2 + \sqrt{3})^2 + 4(-2 + \sqrt{3}) + 1 = 0$$

~~$$4 - 4\sqrt{3} + 3 - 8 + 4\sqrt{3} + 1 = 0$$~~

$$4 + 3 - 8 + 1 = 0$$

$$(-2 + \sqrt{11})^2 + 4(-2 + \sqrt{11}) - 7 = 0$$

~~$$4 - 4\sqrt{11} + 11 - 8 + 4\sqrt{11} - 7 = 0$$~~

$$4 + 11 - 8 - 7 = 0$$

$$[\frac{3(3 + 2\sqrt{5})^2 - 9(\frac{3 + \sqrt{5}}{2}) + 3}{2}] \div 3$$

$$[\frac{9 + 6\sqrt{5} + 5}{4} - \frac{9 + 3\sqrt{5}}{2} + 1 = 0] \times 4$$

~~$$9 + 6\sqrt{5} + 5 - 18 - 6\sqrt{5} + 4 = 0$$~~

$$9 + 5 - 18 + 4 = 0$$

$$(1 + 2\sqrt{3})^2 - 2(1 + 2\sqrt{3}) - 11 = 0$$

~~$$1 + 4\sqrt{3} + 12 - 2 - 4\sqrt{3} - 11 = 0$$~~

$$1 + 12 - 2 - 11 = 0$$